

$$\operatorname{tg} 14x + 3\operatorname{ctg} 14x + \sin 6x - 2\sqrt{2}\sin(3x+P/4) = 4/(\sqrt{3}+1)$$

$$\operatorname{tg} 14x + 3\operatorname{ctg} 14x$$

$$(\operatorname{tg} 14x + 3\operatorname{ctg} 14x)/2 \geq \sqrt{\operatorname{tg} 14x \cdot 3\operatorname{ctg} 14x}$$

$$(\operatorname{tg} 14x + 3\operatorname{ctg} 14x)/2 \geq \sqrt{3}$$

$$(\operatorname{tg} 14x + 3\operatorname{ctg} 14x) \geq 2\sqrt{3}$$

$$(a+b)/2 \geq \sqrt{ab} \quad a=b \quad (a+b)/2 = \sqrt{ab}$$

$$\sin 6x - 2\sqrt{2}\sin(3x+P/4) = -\cos(P/2+6x) - 2\sqrt{2}\sin(3x+P/4) =$$

$$= 2\sin^2(p/4+3x) - 2\sqrt{2}\sin(3x+P/4) - 1 =$$

$$= 2\sin^2(p/4+3x) - 2\sqrt{2}\sin(3x+P/4) + 1 - 2 =$$

$$= [\sqrt{2}\sin(p/4+3x)]^2 - 2[\sqrt{2}\sin(3x+P/4)] \cdot 1 + 1^2 - 2 =$$

$$= [\sqrt{2}\sin(p/4+3x) - 1]^2 - 2$$

$$4/(\sqrt{3}+1) = 4\sqrt{3}-4/2 = 2\sqrt{3}-2 = 2(\sqrt{3}-1)$$

$$\operatorname{tg} 14x + 3\operatorname{ctg} 14x + [\sqrt{2}\sin(p/4+3x) - 1]^2 - 2 = 2\sqrt{3}-2$$

$$\operatorname{tg} 14x + 3\operatorname{ctg} 14x + [\sqrt{2}\sin(p/4+3x) - 1]^2 = 2\sqrt{3}$$

$$[\sqrt{2}\sin(p/4+3x) - 1]^2 = 0$$

$$\sqrt{2}\sin(p/4+3x) - 1 = 0$$

$$\sqrt{2}\sin(p/4+3x) = 1$$

$$\sin(p/4+3x) = 1/\sqrt{2} = \sqrt{2}/2$$

$$P/4+3x = p/4+2pk$$

$$3x = 2pk$$

$$x = 2pk/3$$

$$P/4+3x = 3p/4+2pk$$

$$3x = p/2+2pk$$

$$x = P/6+2pk/3$$

$$\text{Ответ: } x = P/6+2pk/3; x = 2pk/3$$

$$\sin x = \cos(P/2-x)$$

$$\cos x = \sin(P/2-x)$$

$$\operatorname{tg} 14x + 3\operatorname{ctg} 14x = 2\sqrt{3}$$

$$\operatorname{tg} 14x = 3\operatorname{ctg} 14x$$

$$\operatorname{tg} 14x = 3/\operatorname{tg} 14x$$

$$\operatorname{tg} 14x \neq 0$$

$$\operatorname{tg}^2 14x - 3 = 0$$

$$\operatorname{tg} 14x = \pm\sqrt{3}$$

$$14x = \pm p/3 + pn$$

$$x = \pm p/42 + pn/14$$